

$$\mathbf{X} = \hat{\mathbf{X}} + \epsilon = \sum f_i \mathbf{v}_i + \mathbf{b} + \epsilon$$